Intermodulation Mechanism and Linearization of AlGaAs/GaAs HBT’s

Joonwoo Lee, Member, IEEE, Woonyun Kim, Student Member, IEEE, Youngsik Kim, Student Member, IEEE, Taemoon Rho, Member, IEEE, and Bumman Kim, Senior Member, IEEE

Abstract—The intermodulation (IM) mechanism of heterojunction bipolar transistors (HBT’s) has been studied by using an analytical nonlinear equivalent circuit model and Volterra-series analysis of the model. Although the third-order IM intercept point (IP3) does not depend on the emitter parameter, it is appreciably affected by base and collector parameters and has been substantially improved by utilizing punchthrough collector structure. The measured IP3 of punchthrough collector HBT’s is 31 dBm with 150-mW dc power, which is higher than that of normal collector HBT’s by 3 dB. The investigation of the cancellation effects of nonlinear elements reveals that the output nonlinear current components generated by emitter–base current source and base–collector current source cancel each other almost exactly, resulting in high linear characteristics of HBT’s.

Index Terms— Heterojunction bipolar transistors, intermodulation distortion, nonlinear distortion, semiconductor device modeling, Volterra series.

I. INTRODUCTION

AlGaAs/GaAs heterojunction bipolar transistors (HBT’s) are known for their low-distortion characteristics in linear power applications. Third-order intermodulation (IM) intercept points (IP3) as high as 33 dBm have been reported with 150-mW dc power [1], [2]. An internally matched linear-power HBT with 20-W output power, 6.5-dB gain, and 40% power-added efficiency (PAE) at 7.5 GHz was reported and a high-efficiency HBT monolithic-microwave integrated-circuit (MMIC) linear power amplifier for personal communication application has also been demonstrated, where the output power was 21 dBm and PAE was 35% [3], [4]. An ultra-low dc-power HBT low-noise amplifier (LNA) was also reported to have an IP3 level of 22 dBm with 20-mW dc-power consumption at 2 GHz [5].

In spite of the excellent experimental results, the mechanisms responsible for the good linear behavior of AlGaAs/GaAs HBT’s have not been clearly understood. Maas attributed the good IM performance of HBT’s to the exact cancellation of the IM currents between the emitter–base dynamic resistance $r_{je}$ and capacitance $C_{BE}$ [6]. According to [7], the IM currents generated by $r_{je}$ and $C_{BE}$, and the IM currents generated by the total emitter–base current and the total base–collector current are partially canceled. Wang et al. [8] have reported that the feedback effect of the emitter resistance $R_E$ and the base resistance $R_B$ linearized the HBT output power and reduced the third-order IM distortion (IMD3). He also suggested that the $C_{EC}$ nonlinearity caused deterioration of IMD3 performance. From these results, the mechanisms for the nonlinearity of HBT’s are not clearly understood and should, therefore, be clarified. Furthermore, all the reported works used experimentally determined HBT models and could not provide design guidelines for an HBT structure optimized for good linearity.

To clearly understand the IM characteristics of the HBT and to find the optimized linear HBT structure, we have developed an analytical nonlinear HBT equivalent circuit model and computer program calculating IP3 based on Volterra-series analyses [9]–[12]. The simulation results have shown that the punchthrough collector is the best structure for a linearized HBT. Although IP3 does not depend on the emitter structure, it is appreciably affected by base and collector structures. Based on the simulation results, an optimized linear HBT structure has been proposed and its validity has been experimentally demonstrated.

The IM mechanism of the HBT has also been studied by investigating the cancellation effects of IM components generated by nonlinear elements. The output current distortion components generated by emitter–base current source and base–collector current source cancel each other almost exactly, resulting in high linearity. It is also shown that the base–collector capacitance is the key parameter determining the IP3 of an HBT. In Sections II and III, the device nonlinear model is discussed and simulation results are compared with two-tone test results on fabricated HBT’s. In Section IV, cancellation mechanisms of HBT nonlinear components are discussed in detail.

II. NONLINEAR HBT MODEL

The schematic HBT structure used for the analysis is shown in Fig. 1. In this figure, $W_i$, $L_i$, and $W_i$ are the width, length, and thickness of the emitter, base, and collector, respectively.
Fig. 1. Schematic structure of an HBT.

**TABLE I**

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Value</th>
<th>Symbol</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\rho_{BE}$</td>
<td>$1 \times 10^8 , \Omega , \text{cm}^2$</td>
<td>$\varepsilon_{B_{MG}}$</td>
<td>$0.01 \times 10^{-7} , \text{F/cm}$</td>
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<tr>
<td>$\rho_{BC}$</td>
<td>$3 \times 10^8 , \Omega , \text{cm}^2$</td>
<td>$\varepsilon_b, \varepsilon_c$</td>
<td>$1.16 \times 10^{-12} , \text{F/cm}$</td>
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<tr>
<td>$\rho_{CC}$</td>
<td>$1 \times 10^8 , \Omega , \text{cm}^2$</td>
<td>$\Delta E_c$</td>
<td>$0.205 , \text{eV}$</td>
</tr>
<tr>
<td>$L_E$</td>
<td>$20 , \mu\text{m}$</td>
<td>$\Delta E_v$</td>
<td>$0.109 , \text{eV}$</td>
</tr>
<tr>
<td>$L_B$</td>
<td>$24 , \mu\text{m}$</td>
<td>$N_{CD}$</td>
<td>$4.70 \times 10^{11} , \text{cm}^{-3}$</td>
</tr>
<tr>
<td>$L_C$</td>
<td>$24 , \mu\text{m}$</td>
<td>$N_{VA}$</td>
<td>$7.8 \times 10^{14} , \text{cm}^{-3}$</td>
</tr>
<tr>
<td>$S_E$</td>
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<td>$m_0^*$</td>
<td>$0.07 , m_0$</td>
</tr>
<tr>
<td>$S_0$</td>
<td>$2 , \mu\text{m}$</td>
<td>$m_0^*$</td>
<td>$0.5 , m_0$</td>
</tr>
<tr>
<td>$S_C$</td>
<td>$4 , \mu\text{m}$</td>
<td>$\tau_{tr}$</td>
<td>$2.0 \times 10^{-5} , \text{sec}$</td>
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<td>$S_{EB}$</td>
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<td>$V_{TH}$</td>
<td>$0.0259 , \text{V}$</td>
</tr>
<tr>
<td>$S_{BC}$</td>
<td>$2 , \mu\text{m}$</td>
<td>$I_{RB}$</td>
<td>$4.0 \times 10^{-11} , \text{A/cm}^2$</td>
</tr>
<tr>
<td>$S_{COD}$</td>
<td>$7 , \mu\text{m}$</td>
<td>$\eta_B$</td>
<td>$1.92$</td>
</tr>
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</table>

Fig. 2. Nonlinear HBT equivalent circuit model with matching networks.

$$(R_E, R_B, R_C)$$ are calculated from the following equations:

1. $R_E = \frac{\rho_{BC}}{S_{EB} E} + \frac{1}{q\mu_{nE} N_{E} S_{EB} E} W_E$ $\text{Ohm}$  
2. $R_B = \frac{R_{SB} S_{EB}}{12 L_E} + \frac{R_{SB} S_{EB}}{2 L_E} + \sqrt{\rho_{CC} R_{SB}}$ $\text{Ohm}$  
3. $R_C = \frac{R_{SC} S_{CD} L_C}{12 L_C} + \sqrt{\rho_{PC} R_{SC}}$ $\text{Ohm}$  
4. $r_o = \frac{V_A}{I_C} = \frac{\eta_E Q_{FB}}{I_C \eta_{BC}}$ $\text{Ohm}$

where $V_A$ is early voltage, $Q_{FB}$ is total majority carrier charge in the base, and $\eta_E$ and $\eta_C$ are the ideality factors of the emitter and collector junctions, respectively.

The nonlinear elements can be expanded in terms of the node voltages. We considered only up to the third-order
expansion coefficients in the Volterra-series to calculate IP3. The stored charge at base–emitter junction $Q_{be}$ is composed of depletion and diffusion charges and is given by

$$Q_{be} = \sqrt{2e q N_E \left( \sqrt{V_{bi}} - \sqrt{V_{ti}} - V_{be} \right)} A_E + I_e \tau_3$$

(5)

where $\tau_3$ is the base transit time. In the normal operating region, the diffusion capacitance dominates and the effect of the possible error in the depletion capacitance is acceptable. The nonlinear current source $I_e$ is given by [15] and [16] as follows:

$$I_e = I_{Se} \left[ \exp \left( \frac{V_{be}}{V_{TH}} \right) - 1 \right] + I_{RE} \left[ \exp \left( \frac{V_{be}}{\eta_3 V_{TH}} \right) - 1 \right]$$

(6)

where $I_{Se}$ represents the injection current and $I_{RE}$ accounts for the recombination current. Since these parameters depend only on $V_{be}$, they can be expanded as

$$q_{be} = c_{e1} v_{be} + c_{e2} v_{be}^2 + c_{e3} v_{be}^3$$  

$$i_{e} = k_{e1} v_{be} + k_{e2} v_{be}^2 + k_{e3} v_{be}^3$$

(7)

(8)

where the $q_{be}$, $v_{be}$, and $i_{e}$ are the small-signal components of $Q_{be}$, $V_{be}$, and $I_e$, respectively. The coefficients in the above equations are given by the Taylor-series expansion of $Q_{be}$ and $I_e$ with respect to $V_{be}$.

The nonlinear base–collector capacitance $C_{BC}$ was modeled as

$$W_d = \sqrt{2 e (V_{bi} + V_{cb}) / q N_C}$$

$$C_{BC} = \frac{e A_C}{W_d}, \quad \text{for } W_d \leq W_C$$

$$C_{BC} = \frac{e A_C}{W_C}, \quad \text{for } W_d > W_C$$

(9)

(10)

where $A_C$ is the collector area. The stored charge at the base–collector junction $Q_{bc}$ is dependent only on $V_{cb}$, so the small-signal component $q_{bc}$ can be expanded as follows:

$$q_{bc} = c_{b1} v_{cb} + c_{b2} v_{cb}^2 + c_{b3} v_{cb}^3$$

(11)

where the coefficient $c_{bi}$ is the Taylor-series expansion of $Q_{bc}$ with respect to $V_{cb}$. The small-signal current can be obtained by taking the time derivative of $q_{bc}$. The nonlinear current source at the base–collector junction $I_c$ is given by

$$I_c = \alpha I_e$$

(12)

The common base current gain $\alpha$ can be written as

$$\alpha = \sqrt{2 e q N_C / \omega_b}$$

(13)

where $\tau$ and $\omega_b$ are the base–collector transit time and cutoff frequency, respectively. The dc current gain $\alpha_0$ was modeled as in [15]–[18]. Since $I_e$ and $\alpha_0$ depend only on $V_{be}$, the small-signal component of the collector current can be represented as follows:

$$i_c = k_{c1} v_{be} + k_{c2} v_{be}^2 + k_{c3} v_{be}^3$$

(14)

where $k_{ci}$ is the Taylor-series expansion of $I_c$ with respect to $V_{be}$. By using all the above expansion coefficients, the node equations in the HBT equivalent circuit of Fig. 2, can be found as

$$\frac{v_{b}}{Z_m} = \sum_{i=1}^{3} \left( k_{ci} - j \omega \omega_c \right) v_{be}^i - \sum_{i=1}^{3} j \omega \omega_c v_{be}^i$$

$$0 = \frac{v_2}{R_E} - \sum_{i=1}^{3} \left( k_{ci} - j \omega \omega_c \right) v_{be}^i + \frac{v_{b}}{r_0}$$

(15)

where $v_{b} = v_i - v_j$, and $Z_m$ and $Z_o$ are indicated in Fig. 2. The $i$th-order transfer function is obtained directly from the above node equations for each $i$ (= 1, 2, 3). The linear components $Z_m$, $Z_o$, $R_E$, $R_B$, $R_C$ and $r_0$ are included only in the first-order transfer function.

### III. DESIGN OF THE LINEARIZED HBT’S

#### A. Simulation Results

To find out the optimum HBT structures maximizing IP3, we have investigated the IP3 dependence of HBT structures under various bias conditions ($I_{CE}$, $V_{CE}$). A two-tone simulation was performed as a function of $N_E$, $P_B$, $N_C$, $W_E$, $W_B$, and $W_C$ at frequencies $f_1 = 10$ GHz and $f_2 = f_1 + \Delta f$, where $\Delta f = 10$ MHz. We applied simultaneous conjugate matching conditions to the simulation because power matching cannot be implemented for the analysis. The simulation results are shown in Fig. 3, under bias condition of $V_{CE} = 3$ V and $I_C = 24$ mA ($J_C = 4 \times 10^4$ A/cm$^2$).

Fig. 3(a) shows IP3 dependence on the collector doping and thickness. The base doping and thickness are $2 \times 10^{19}$ cm$^{-3}$ and 0.1 $\mu$m, respectively. It should be noted that IP3 is very high when the collector is fully depleted. The IP3 of punchthrough collector devices is about 10 dB higher than that of the normal device. The discontinuities in the IP3 lines due to the transition from the collector punchthrough region to the nonpunchthrough region for the given bias. We have observed similar behavior at different bias conditions. The base-structure dependency on IP3 performance is shown in Fig. 3(b). The collector doping is $2 \times 10^{19}$ cm$^{-3}$ and the collector thicknesses is 1.0 $\mu$m. As shown in Fig. 3(b), IP3 weakly depends on the base thickness, but it is rather strongly dependent on base doping. For $W_B = 0.1$ $\mu$m, it improves by about 3 dB as the base doping decreases from $3 \times 10^{19}$ cm$^{-3}$ to $1 \times 10^{19}$ cm$^{-3}$. In the widely used range of base doping and thickness, IP3 of the chosen device is between 24–28 dBm. Fig. 3(c) shows IP3 dependence on the emitter doping. The base and collector dopings are $2 \times 10^{19}$ cm$^{-3}$ and $2 \times 10^{16}$ cm$^{-3}$, respectively, and the emitter, base, and collector
thicknesses are 0.2, 0.1, and 1.0 μm, respectively. Thus, IP3 is insensitive to the emitter doping, in agreement with the results of Wang et al. [8].

From the above simulation results, IP3 performance of the HBT does not strongly depend on the emitter parameters, while it is appreciably dependent on base and collector parameters. In particular, the device linearity is remarkably improved in the punchthrough collector structure. We have utilized the simulation results in choosing three HBT structures for our experiment. HBT2 is a typical power-structure HBT with \( W_B = 0.1 \mu m \) and \( W_C = 1.0 \mu m \). To verify the base-structure effect on IP3 performance, the base thickness of HBT3 was chosen to be 0.14 μm. HBT1 is the punchthrough collector structure HBT with \( W_C = 0.4 \mu m \). Since IP3 is not sensitive to emitter parameters, all three HBT’s have the same emitter doping \( 2 \times 10^{18} \text{cm}^{-3} \) and thickness \( 0.2 \mu m \). The doping concentrations of the base and collector are \( 2 \times 10^{19} \text{cm}^{-3} \) and \( 2 \times 10^{16} \text{cm}^{-3} \), respectively.

Fig. 4(a) and (b) show IP3 performances of HBT1 and HBT2 as functions of the applied biases. We can see that IP3 is more sensitive to the collector-bias voltage than to the collector-bias current. It suggests that the base–collector capacitance \( C_{BC} \) is the key element determining IP3 performance of HBT. Note that the IP3 value of HBT1 is remarkably improved...
at punchthrough bias condition. It has the same IP3 value as HBT2 when the collector is not fully depleted. HBT3 showed similar IP3 performance to HBT2. However, its IP3 level was slightly lower than that of HBT2 at the same bias voltage.

B. Two-Tone Test Results

We have fabricated AlGaAs/GaAs HBT’s using the self-aligned base metal (SABM) process technique. The epilayer structures designed from the above simulation were used. Our HBT structure, process, and main dc/RF performances were reported in detail elsewhere [19].

The two-tone test has been performed to characterize the linearity of the three HBT’s. An HP8350B Sweep Oscillator was used as an RF source and FOCUS1808 Programmable Tuner was used to match the devices. The input frequencies of two RF sources were selected at 10 and 10.01 GHz. The HBT’s was biased with an HP6626A dc Power Supply and output power level was measured using an HP8562A Spectrum Analyzer. The characterization system was automatically controlled by the computer connected to the measurement setup. The IP3 level of the devices were obtained by extrapolating $P_1$ and $P_3$ powers at a linear gain region.

Fig. 5(a)–(c) shows the two-tone test results of the devices under the same bias condition of $I_C = 15$ mA and $V_{CE} = 3$ V. The main results have been summarized in Table II. As shown in the figure, two HBT’s with normal collectors exhibit similar performance. At the 1-dB gain compression point, the IMD3 of the HBT2 is $-33 \text{ dBc}$ with output power of 9.5 dBm and that of HBT3 is $-32 \text{ dBc}$ with output power of 10.1 dBm. The IP3 level of the devices extrapolated from the linear gain region is 28 dBm, which corresponds to linearity figure of merit (LFOM $= IP3/P_{1\text{dB}}$) of 14 [8]. For HBT1 with punchthrough collector, IMD3 is $-36 \text{ dBc}$ with output power of 10.1 dBm. The IP3 value of the device is 31 dBm, which corresponds to an LFOM of 28 and is higher than that of HBT2 or HBT3 by 3 dB. Compared with the simulation results, the measured IP3 of the normal collector HBT is higher by 3 dB, while that of HBT1 is lower by 4 dB. The main cause of the differences between experimental and simulation results can be attributed to the fact that the simulation was performed at the small-signal gain matching condition. However, it is clear that the punchthrough collector device exhibits better IP3 performance than the normal collector device.

IV. CANCELLATION MECHANISM OF HBT NONLINEAR COMPONENTS

As mentioned earlier, it is not clear why HBT’s exhibit good linearity in spite of the presence of strong nonlinear components. To clearly understand the nonlinear mechanism of HBT’s, we have investigated the contribution of the nonlinear elements to IP3. The typical power HBT structure (HBT2) was chosen for the simulation. First, the effects of each nonlinear element of an HBT have been studied by artificially linearizing the nonlinear element under consideration. Next, the cancellation mechanisms among the nonlinear components were investigated by considering only two nonlinear elements at a time.
Fig. 5. Measured power-added efficiency, fundamental, and third-order output powers of HBT's as a function of input power ($I_C = 15$ mA and $V_{CE} = 3$ V). (a) HBT1. (b) HBT2. (c) HBT3.

Fig. 6(a) and (b) shows the IP3 performance of the HBT when the base-emitter nonlinear current source $I_e$ or the collector current source $I_c$ is substituted by a linear element. Compared with the normal HBT with all nonlinear elements, the IP3 level falls off by a large amount in the low collector-bias region [see Fig. 4(b)]. In these cases, IP3 depends on the collector current as well as the collector-bias voltage. However, as shown in the Fig. 6(c), IP3 is improved by more than 13 dB by eliminating the nonlinearity of base-collector capacitance $C_{BC}$. Note that IP3 is more sensitive to the collector current than the collector voltage because $C_{BC}$ nonlinearity originating from the collector-bias voltage is eliminated. When the third-order component of the nonlinear current generated by $C_{BE}$ source was removed by treating it as a linear element, the IP3 level of HBT was reduced by less than 1 dB from that of normal HBT. This result indicates that $C_{BE}$ is not a key element in determining IP3 level, in agreement with the previous results of Section III.

Fig. 6(d) shows IP3 performance when both $I_e$ and $I_c$ are treated as linear elements and only $C_{BE}$ and $C_{BC}$ are operated as nonlinear sources. Note that their IP3 performances are quite similar to the result of the normal HBT with all nonlinear sources except for the very low collector-bias current region. As previously pointed out, IP3 appreciably falls off if one of the third-order nonlinear currents generated by the $I_e$ and $I_c$ sources was eliminated. This indicates that the harmonic components generated by two nonlinear current sources of $I_e$ and $I_c$ cancel each other almost exactly, resulting in high linearity. We have also investigated the cancellation effects of other components, but there were no other significant cancellation effects between IM currents.
V. CONCLUSION

An analytical nonlinear HBT equivalent circuit model and computer program for calculating IP3 have been developed to understand the IM characteristics of HBT’s and to find the optimized linear HBT structure. The simulation results have shown that IP3 performance of the HBT does not strongly depend on the emitter parameters, while the performance is appreciably dependent on base and collector parameters. In particular, the device linearity has been dramatically improved using the punchthrough collector structure.

The collector punchthrough device exhibited an IP3 level of 31 dBm, which was 3 dB higher than that of normal collector HBT’s. Based on simulation results, we have proposed an optimized linear HBT structure. The investigation of the cancellation mechanisms among the nonlinear components has shown that the harmonic components generated by the emitter-base current source and base-collector current source cancel each other out almost exactly, resulting in high linearity of the HBT. $C_{BE}$ does not affect the HBT linearity, but $C_{BC}$ is a very strong nonlinear source and should be linearized using the punchthrough collector structure for reduced distortion.
REFERENCES


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